



# **Gas Turbine Components and Simulation GT Performance Short Course (Montreal 21-24 Sep 2022)**

**Dr. Suresh Sampath**  
**Propulsion Engineering Centre**

[www.cranfield.ac.uk](http://www.cranfield.ac.uk)

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## Topic Overview

- Overview of dimensionless parameters
- Understanding Component characteristics (maps)
- Design Point Simulation
- Off-Design point simulation.



# Components of a Gas Turbine

- Intake
- Compressor/Fan/Booster
- Combustor
- Turbine/Power Turbine
- Nozzle
- Jetpipe/Reheater
- Intercooler
- Recuperator



# Dimensionless Analysis

- Engine performance → described by many variables + operating envelope
- E.g. mass flow  $\dot{W}$  is a function of:

Parameters
Tamb
Pamb
Ma
N
D-engine
R (working fluid)
$\gamma$ (working fluid)
Viscosity

Dimensionless group
Dimensionless group for N
Ma
Dimensionless group for viscosity (2 <sup>nd</sup> order effect)

## Parameters definition

	Full-dimensionless	Semi-dimensionless (quasi-dimensionless)	Referred (corrected)
Mass flow W	$\frac{W \sqrt{R T_1 / \gamma}}{D^2 P_1}$	$\frac{W \sqrt{T_1}}{P_1}$	$CM = \frac{W \sqrt{\theta}}{\delta}$
Rotational speed (N)	$\frac{N}{\sqrt{\gamma R T_1}}$	$\frac{N}{\sqrt{T_1}}$	$\frac{N}{\sqrt{\theta}}$

$$\Delta (\delta) = P_1 / 101.325 \text{ kPa}$$

$$\Theta (\theta) = T_1 / 288.15 \text{ K}$$

$$CN = \frac{\frac{N}{\sqrt{T_1}}}{\left( \frac{N}{\sqrt{T_1}} \right)_{design}}$$

CN: relative to the DP value

$$PCN = N / N_{design}$$

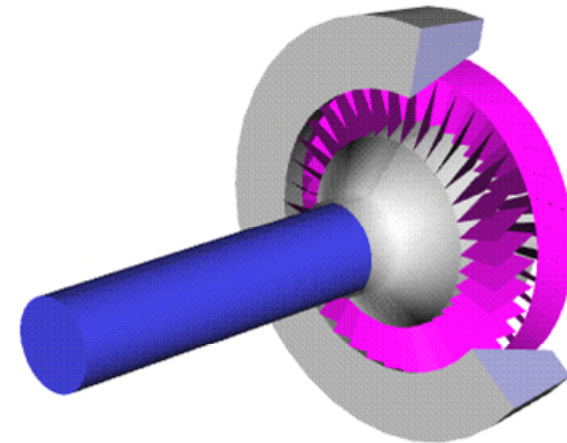
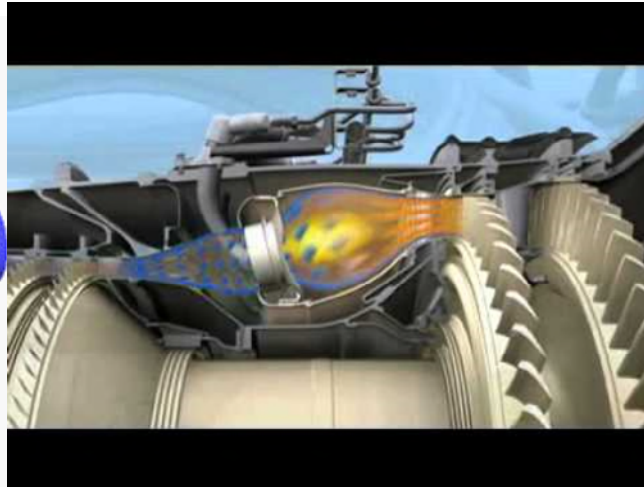
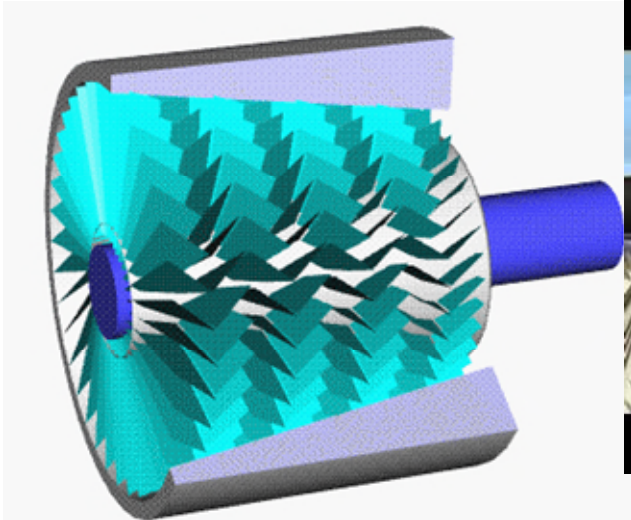


## Design Point Definition

- The “size” of a gas turbine engine is usually defined by  $W$  and  $PR$ .
- $W$ ,  $PR$ ,  $TET$  can be determined for a given power output from preliminary calculations.
- The engine components are designed in detail to give required **Design Point (DP)** performance.
  - the particular **point** in the **operating range** of a gas turbine when the engine is running at the particular **speed, pressure ratio and mass flow** for which the engine components were **designed**.
- Baseline Vs DP performance?

## Off-Design Point Definition

- Off-Design performance (OD): its overall performance over the entire operating range of speed and power output.
- OD performance:
  - determined by the interaction of the components (i.e. matching)
  - Each component → wide operating range → interaction (matching) → this will restrict the operating range



Courtesy of Wikipedia

## Simulation importance

- Why is simulation important? (i.e. engine's performance under different operating conditions?)
- economic and safety, e.g.:



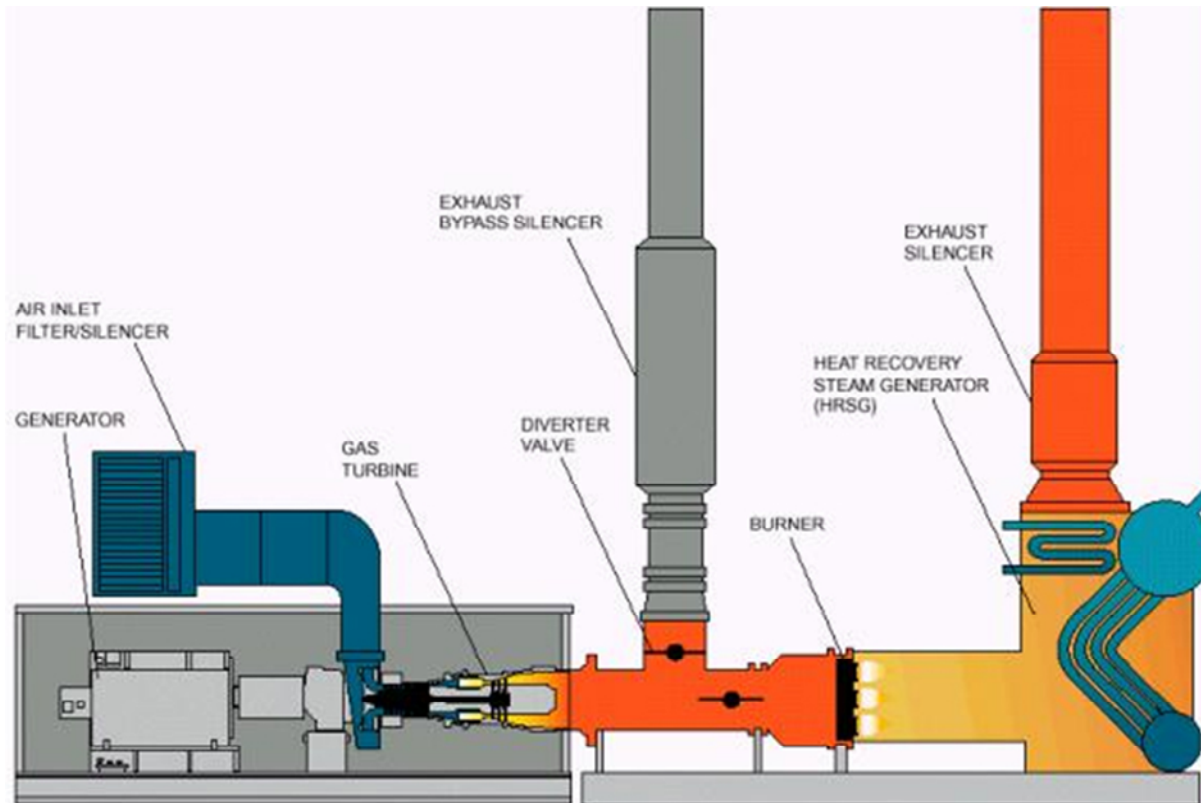
[http://en.wikipedia.org/wiki/Boeing\\_767](http://en.wikipedia.org/wiki/Boeing_767)

Idle conditions  
i.e. different power settings  
SFC?



## Simulation importance

- Why is simulation important? (i.e. engine's performance under different operating conditions?)
- economic and safety, e.g.:



Part load  
SFC?  
£?  
Life?

## Simulation importance

- Why is simulation important? (i.e. engine's performance under different operating conditions?)
- economic and safety, e.g.:



[http://www.coal2nuclear.com/s2\\_6-8\\_medium.htm](http://www.coal2nuclear.com/s2_6-8_medium.htm)

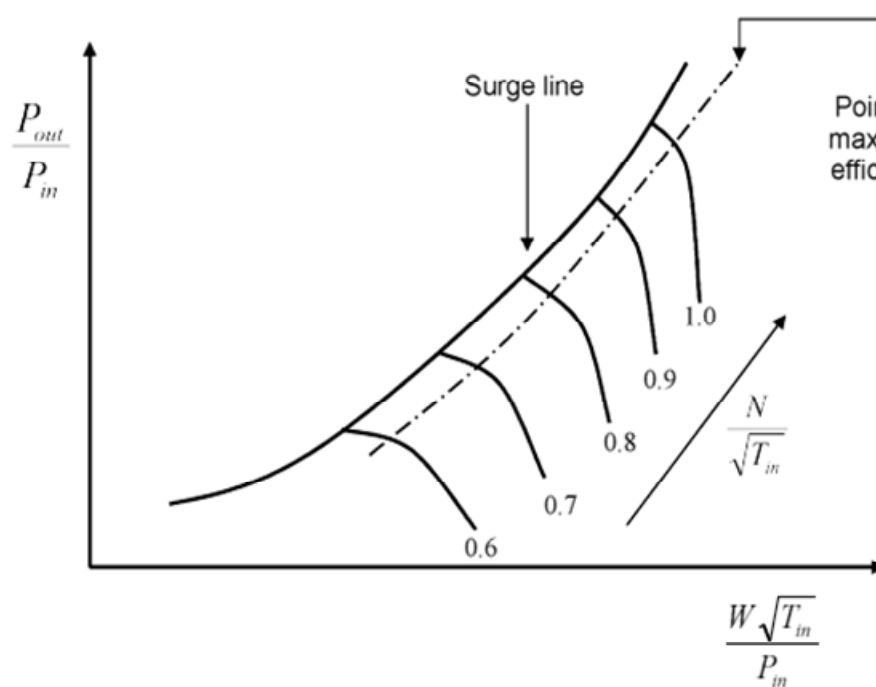
Ambient conditions  
Temperature  
Pressure  
Altitude



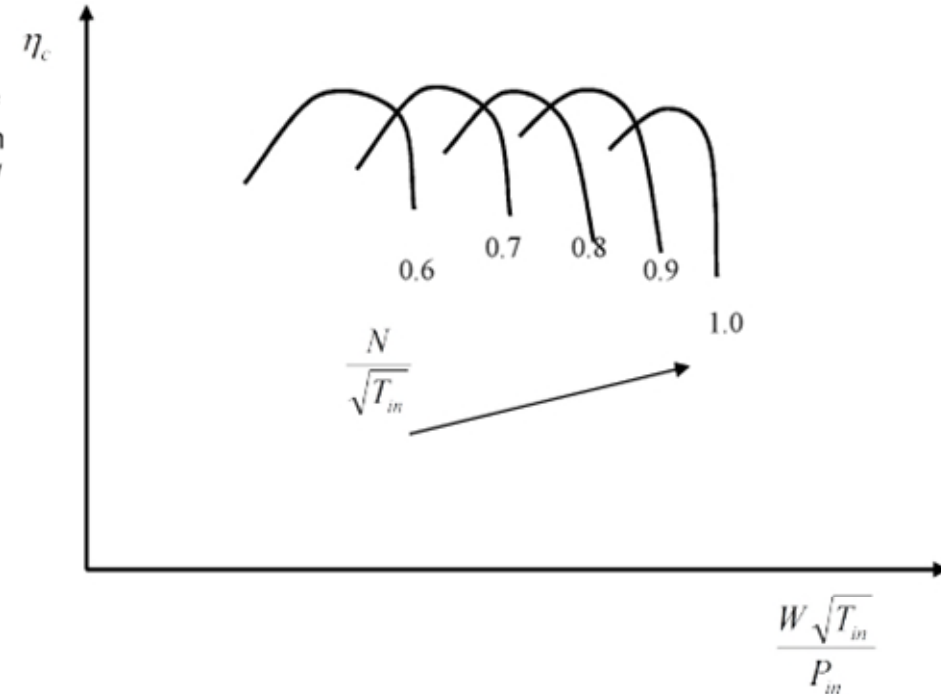
## Component characteristics

- Component characteristics (maps) determine component's performance parameters
  - Compressor
  - Combustor
  - Turbine
  - Propelling nozzle
- Critical role in the OD “matching” of the engine.

# Axial Compressor Characteristics



Pressure ratio Vs. non-dim. mass flow

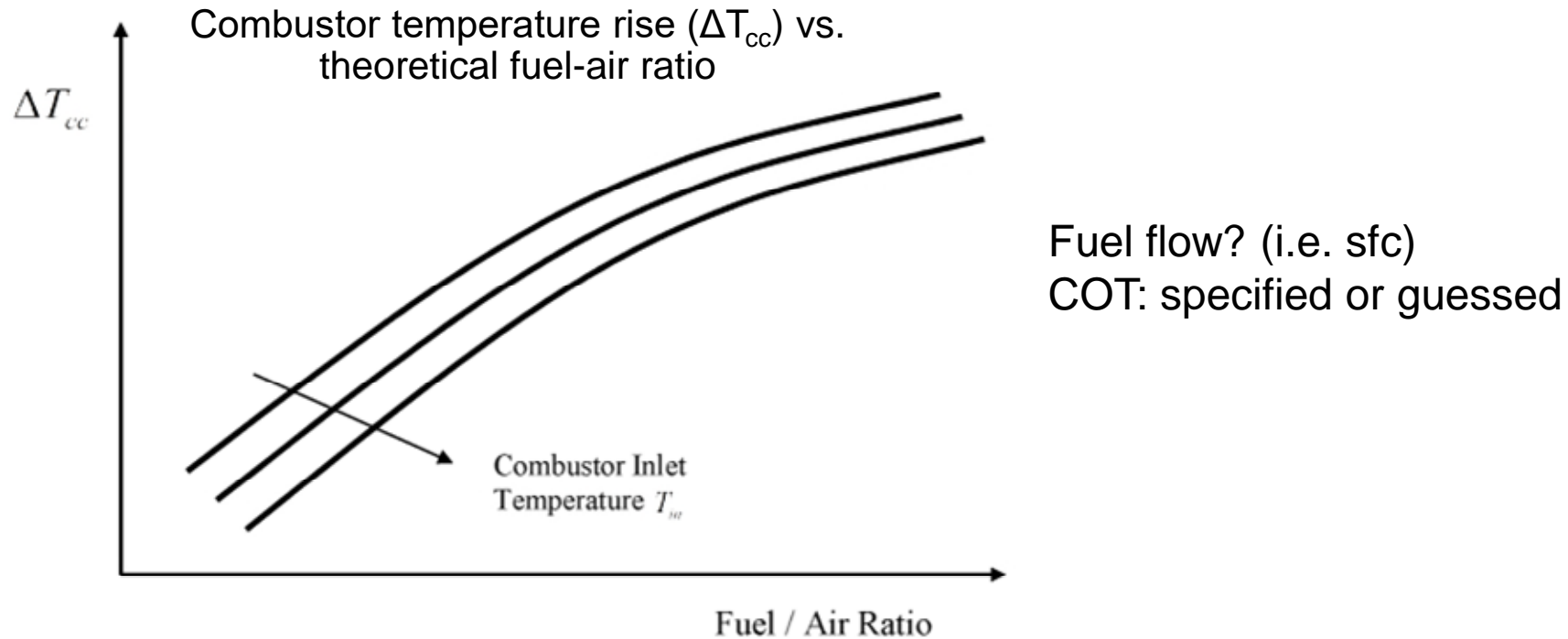


Efficiency Vs. non-dim. mass flow

- Narrow range of  $W$  for a given  $N/\sqrt{T}$  (vertical lines)
- DP is close to the surge line

$N/\sqrt{T}$  is usually relative to design value

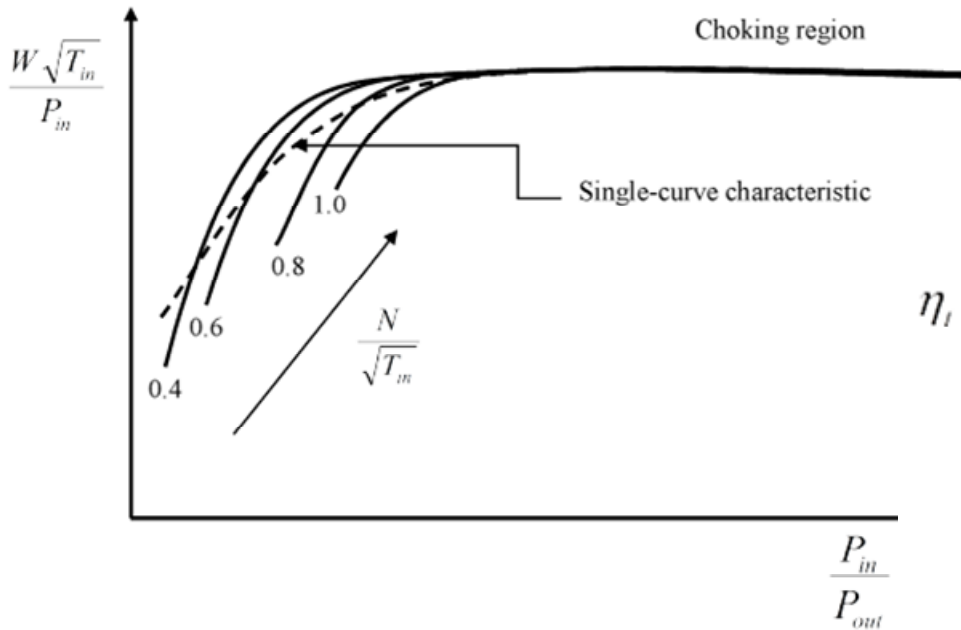
## Combustor characteristics



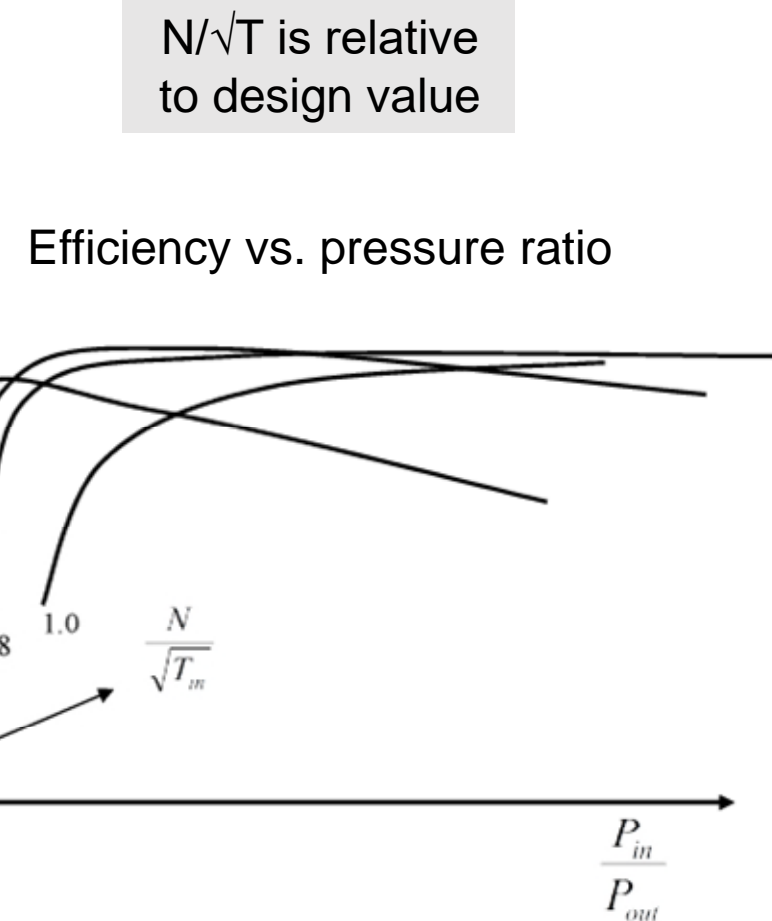
### Combustion Efficiency

- for a given  $\Delta T$  :  $\eta_{cc} = \text{FAR}_{\text{theoretical}} / \text{FAR}_{\text{actual}}$
- for a given FAR:  $\eta_{cc} = \Delta T_{\text{actual}} / \Delta T_{\text{theoretical}}$

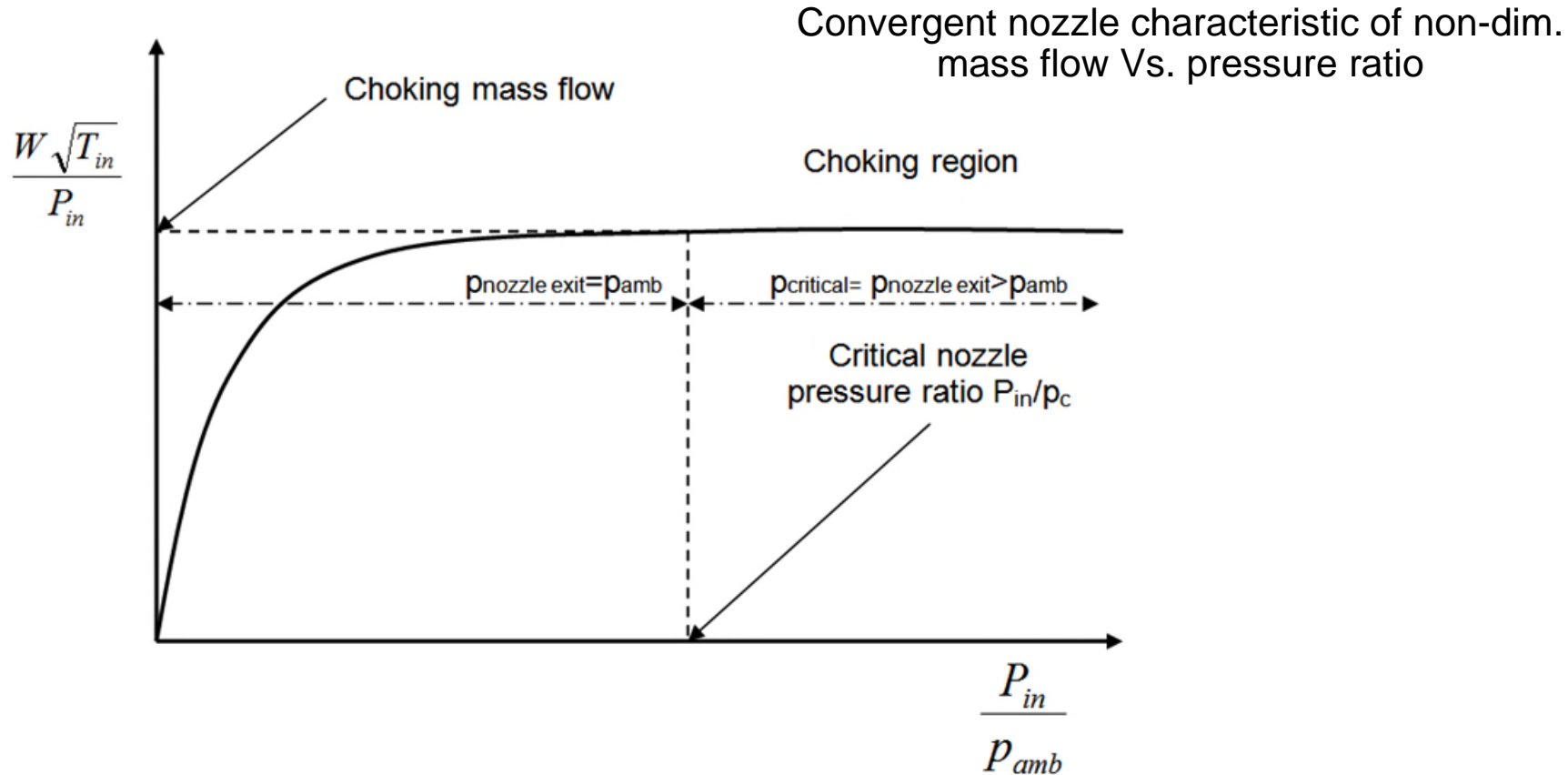
# Turbine characteristics



Non-dim. mass flow vs. pressure ratio

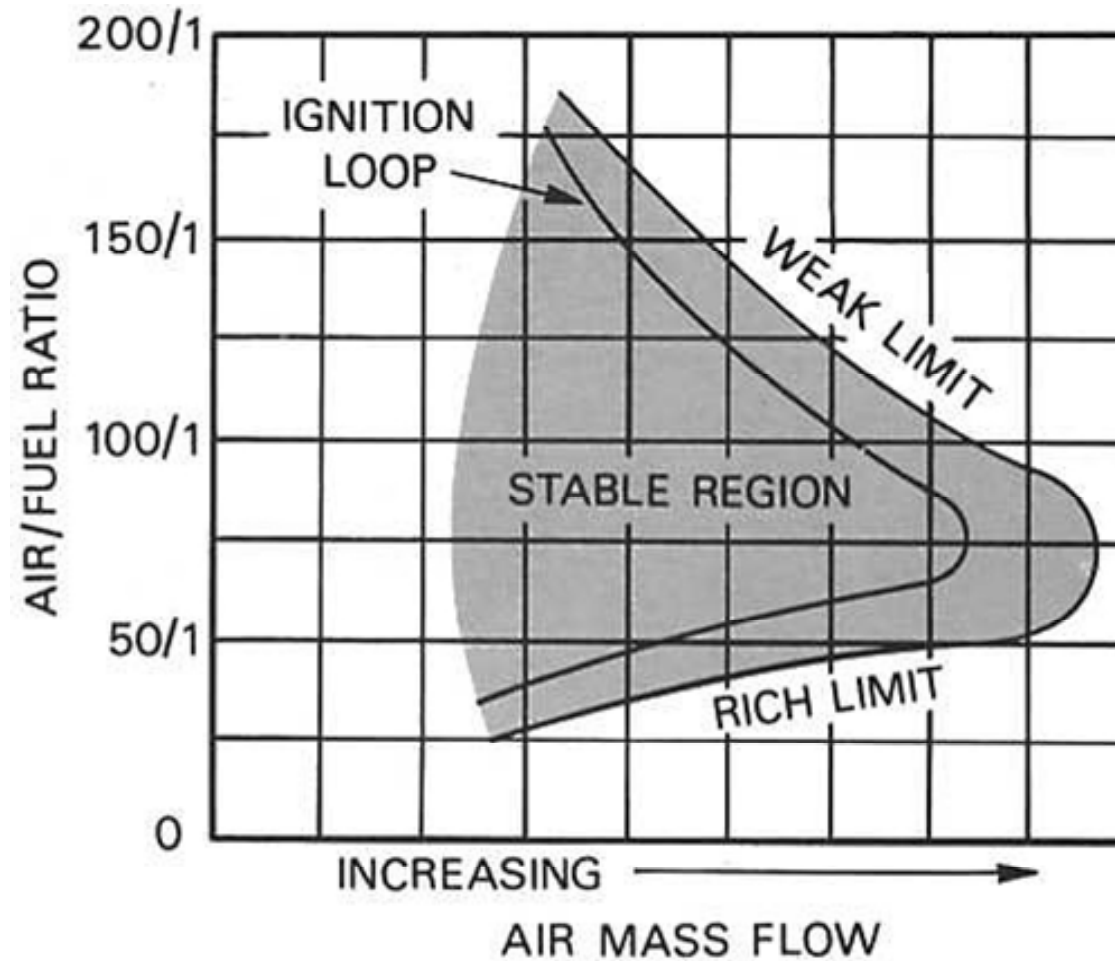


# Propelling nozzle



- Nozzle area is obtained from the DP calculations and remains fixed in OD calculations (not in variable-area nozzle)
- Exit static pressure =, or > ambient pressure (con nozzle).

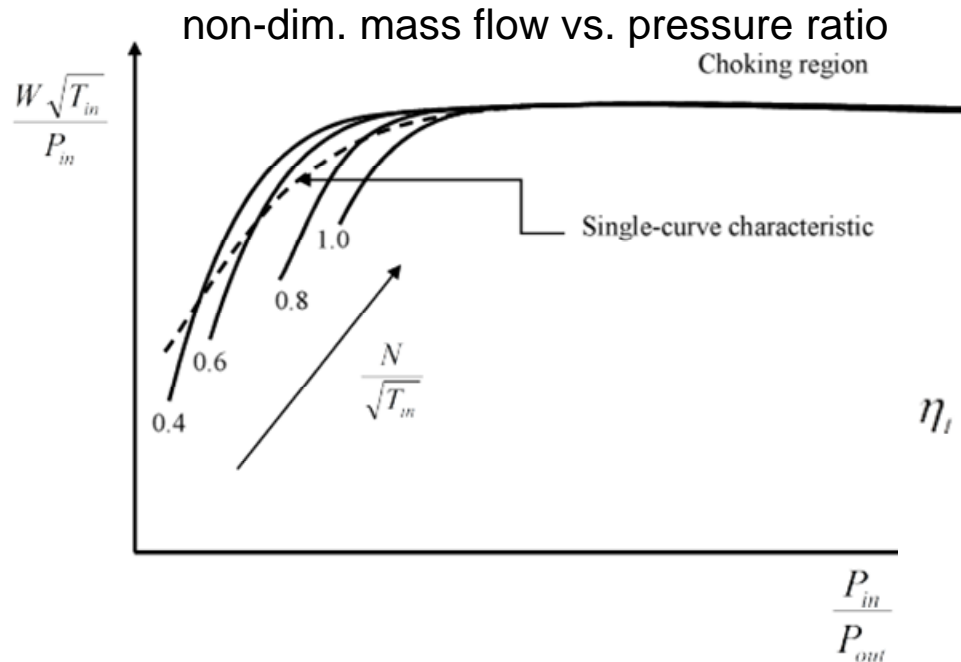
# Combustion Stability





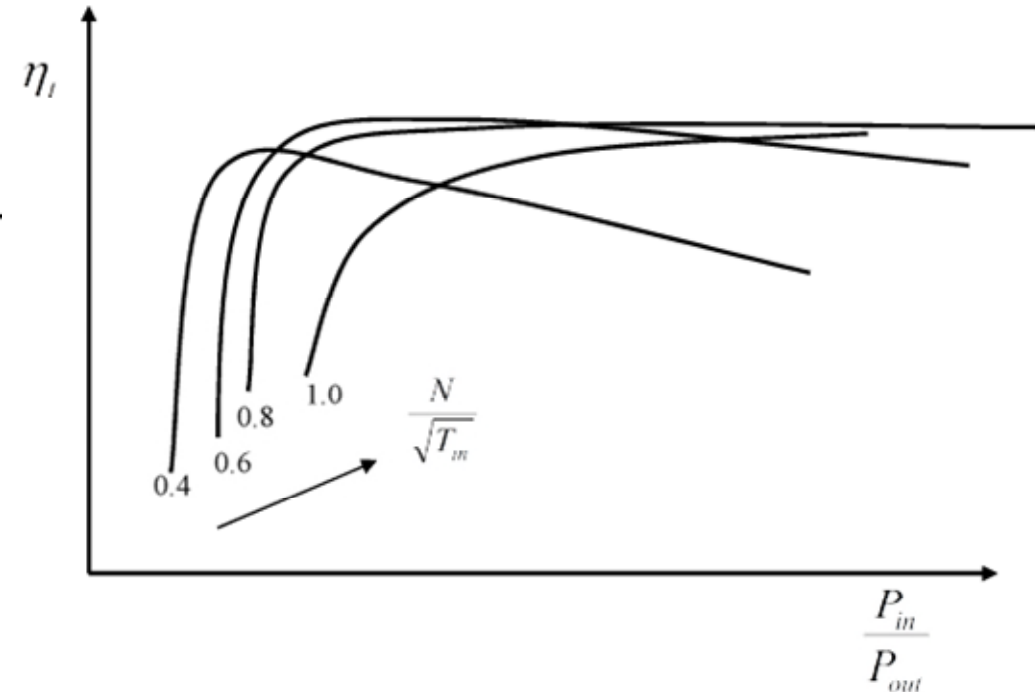
# Component Characteristics

Turbine characteristic of



They are sufficient to describe turbine performance under different operating conditions.

Turbine characteristic of efficiency vs. pressure ratio



# Gas Turbine Nozzle

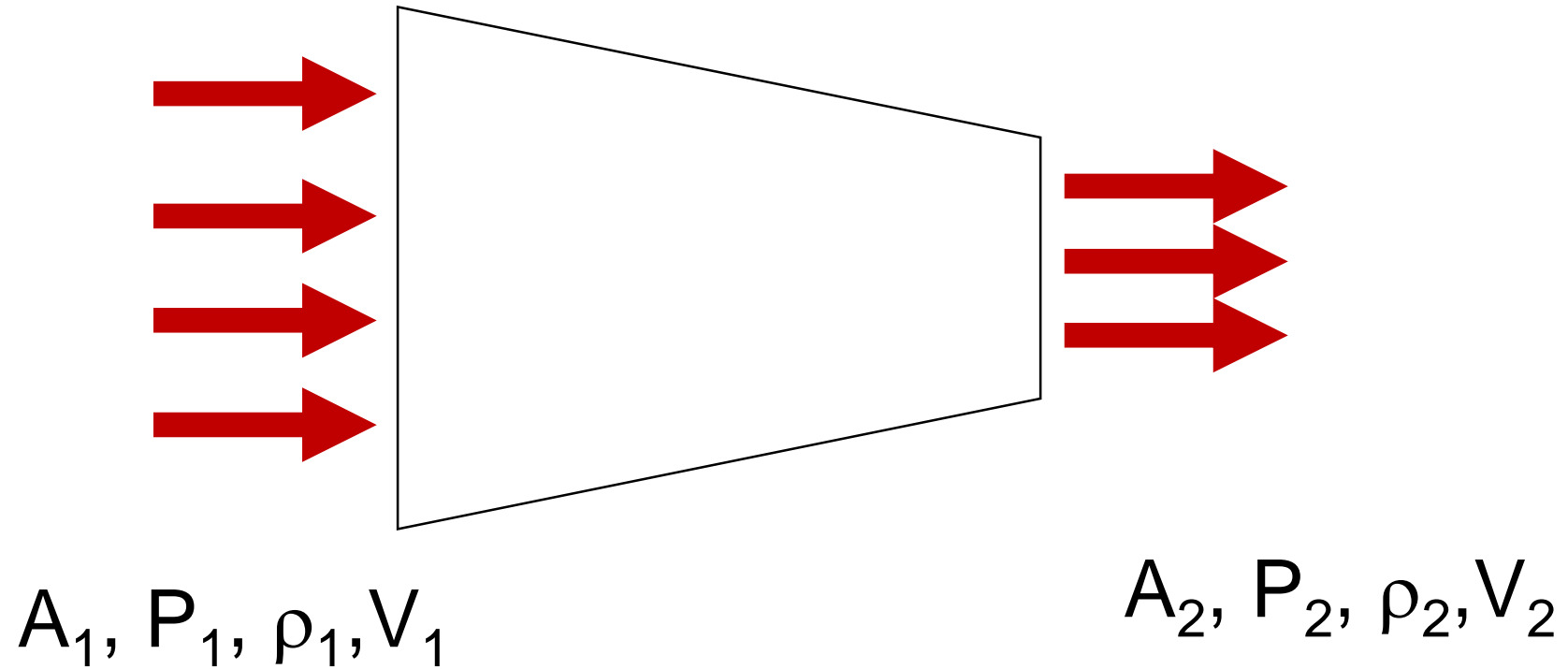


Image courtesy GE

# Gas Turbine Nozzle

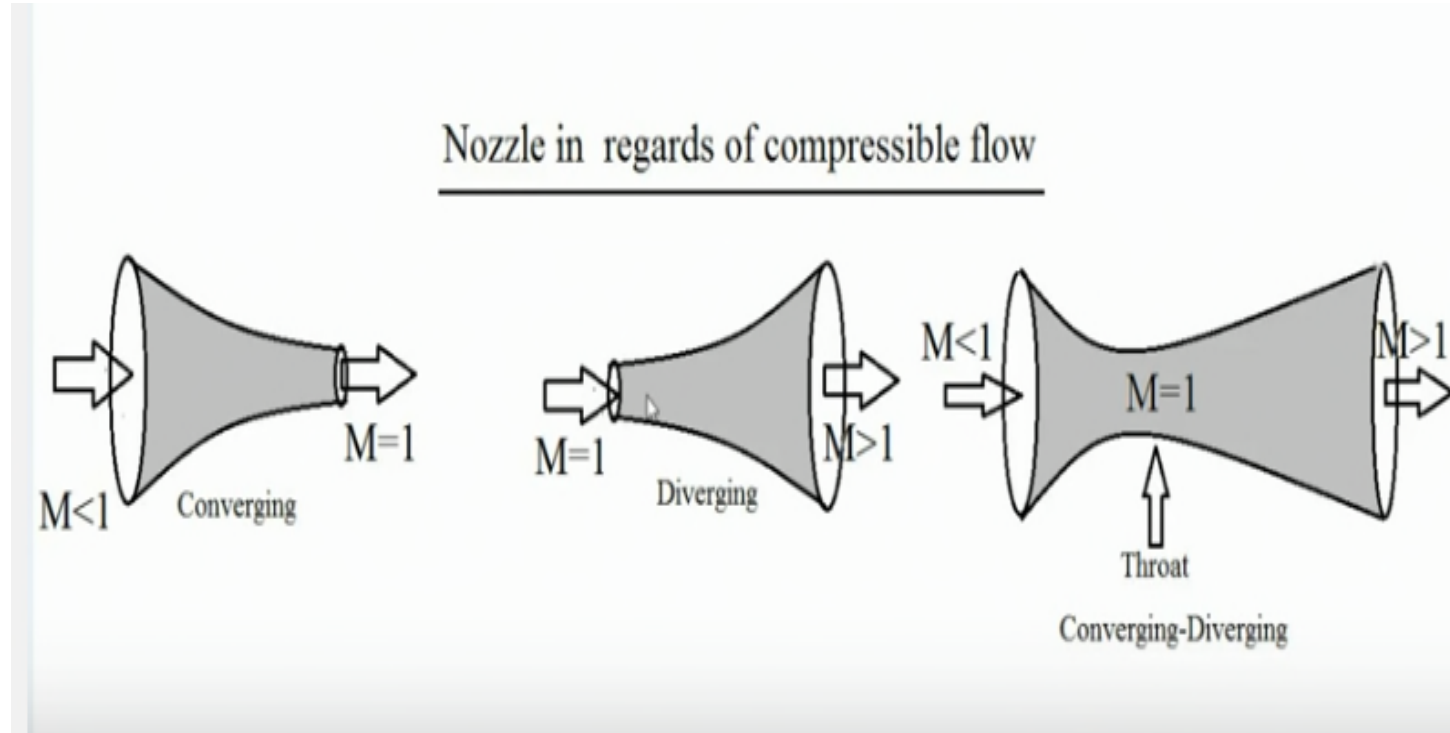


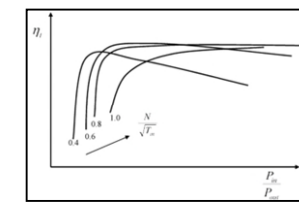
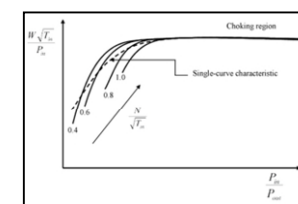
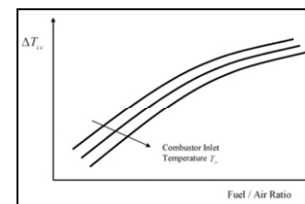
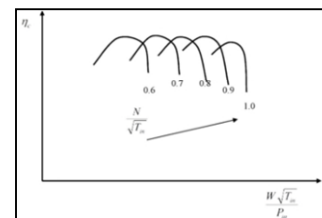
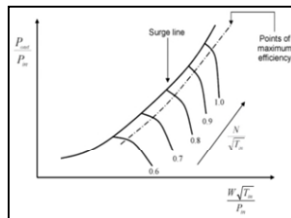
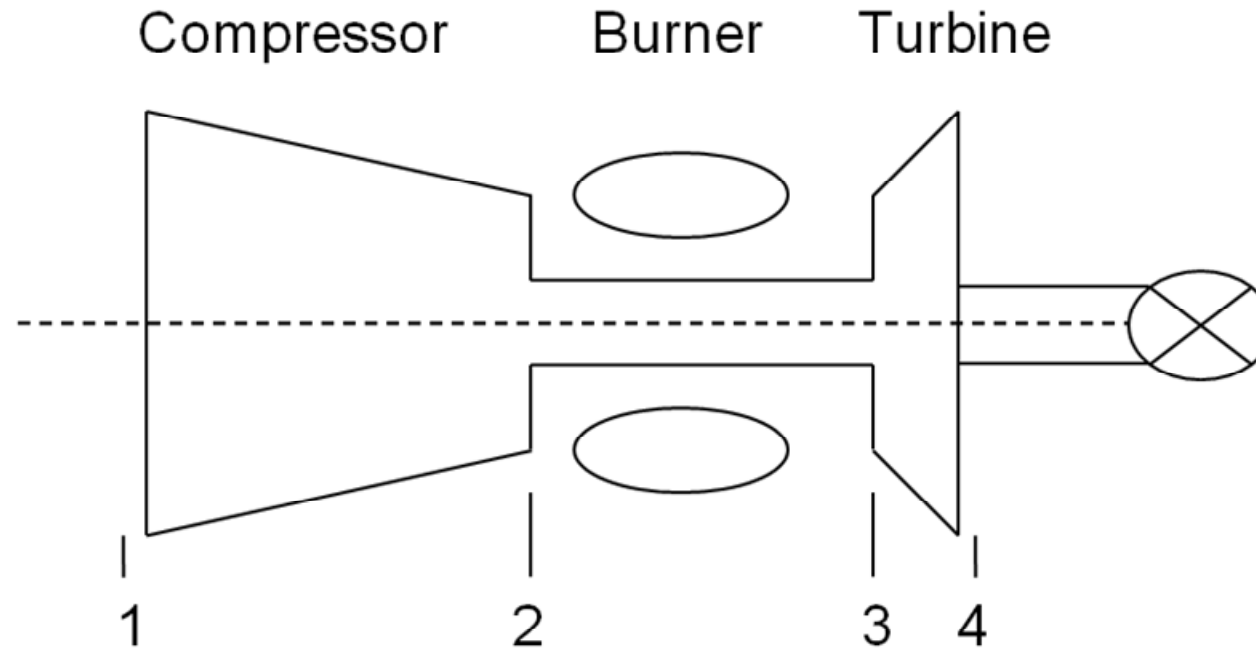
Image courtesy GE



## Engine Steady State Conditions

- Essential conditions of compatibility must be satisfied between the various components of an engine:
  - Mass flow
  - Work
  - Rotational speed
- OD performance simulation: **a “handle” is needed**

# Engine Simulation





## Engine steady state conditions

- A direct solution to obtain the OD performance is not possible.
- It requires:
  - Iterative procedure
  - All engine variables are consistent with the “handle”
  - Some engine parameters are **guessed**
  - Checks are carried out to ensure that the results are compatible with the engine characteristics (“errors” should tend to 0).



## Iterative methods

- Drawbacks:
  - Loops are nested (inner loop repeated for outer loops – increased number of iteration)
  - computationally inefficient

**Matrix solution method is more common**

**Newton Raphson Method**



## Matrix Iteration

- The equations are formed by changing one variable and calculating the errors it produces.
- In matrix iteration the equations are solved simultaneously.
- $\text{Error} = (\text{calculated value} - \text{map value}) / (\text{map value})$



## Iterative methods

*i = number of variables*

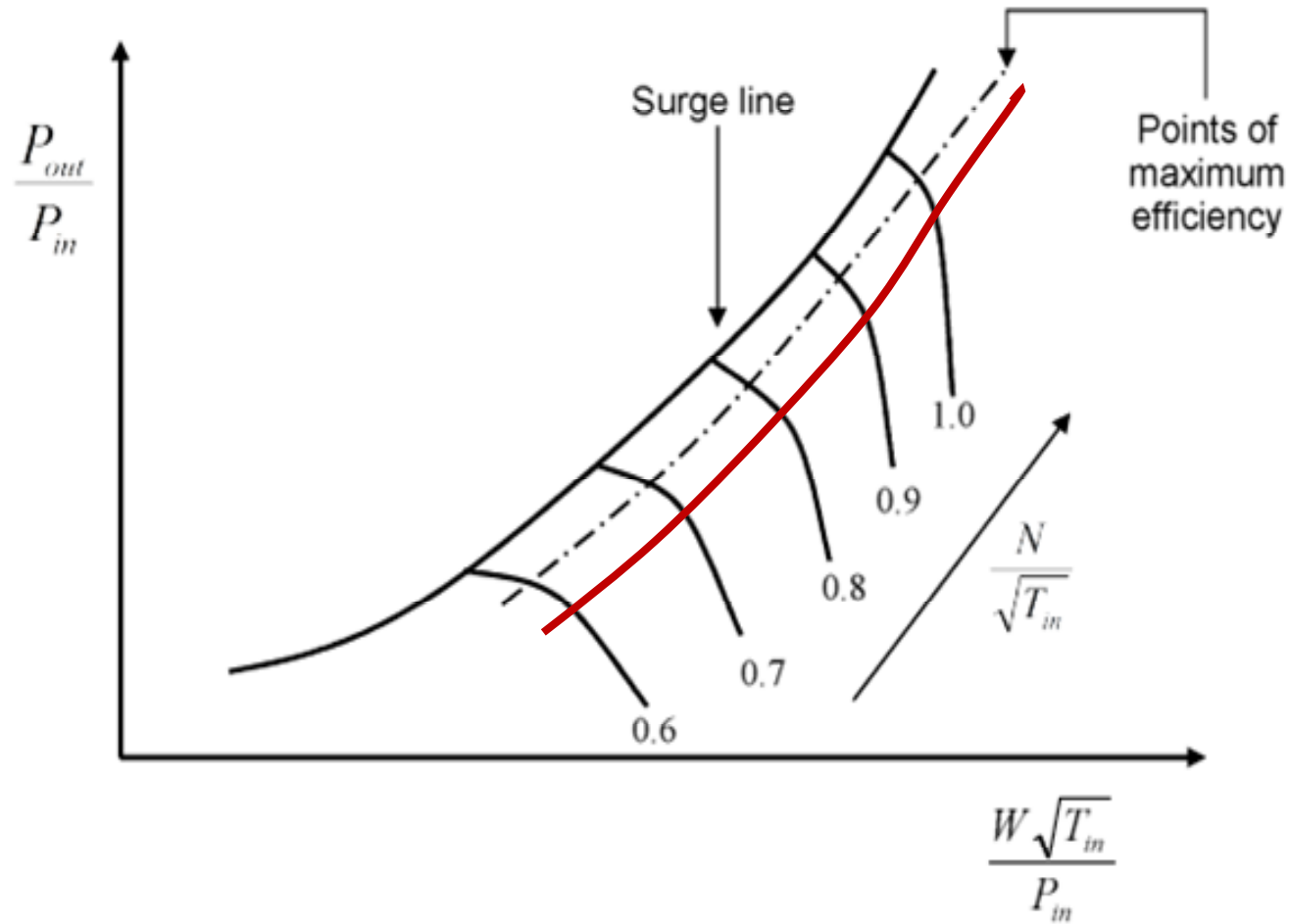
*j = number of errors*

$$\begin{array}{l}
 EB_1 = E_{11}dV_1 + E_{12}dV_2 + \cdots + E_{1j}dV_j \\
 EB_2 = E_{21}dV_1 + E_{22}dV_2 + \cdots + E_{2j}dV_j \\
 \dots \dots \\
 \dots \dots \dots \\
 EB_j = E_{i1}dV_1 + E_{i2}dV_2 + \cdots + E_{ij}dV_j
 \end{array}$$

Eij: change in error Ei caused by a change in variable Vj

Always: i=j

# Engine Working Line





*Thank You*

Email: [s.sampath@cranfield.ac.uk](mailto:s.sampath@cranfield.ac.uk)

Phone: +44-1234-754712